

# 1 Estimating fish population abundance by integrating quantitative 2 data on environmental DNA and hydrodynamic modeling

3 Running head: Estimating population abundance using eDNA

4 Keiichi Fukaya,<sup>1,2\*</sup> Hiroaki Murakami,<sup>3</sup> Seokjin Yoon,<sup>4</sup> Kenji Minami,<sup>5</sup> Yutaka Osada,<sup>6,7</sup>  
Satoshi Yamamoto,<sup>8</sup> Reiji Masuda,<sup>3</sup> Akihide Kasai,<sup>4</sup> Kazushi Miyashita,<sup>9</sup>  
Toshifumi Minamoto,<sup>10</sup> and Michio Kondoh<sup>6\*\*</sup>

<sup>1</sup>*National Institute for Environmental Studies, Tsukuba, Ibaraki 305-8506, Japan*

<sup>2</sup>*The Institute of Statistical Mathematics, Tachikawa, Tokyo 190-8562, Japan*

<sup>3</sup>*Maizuru Fisheries Research Station, Field Science Education and Research Center, Kyoto University,  
Maizuru, Kyoto 625-0086, Japan*

<sup>4</sup>*Faculty of Fisheries Sciences, Hokkaido University, Hakodate, Hokkaido 041-8611, Japan*

<sup>5</sup>*Estuary Research Center, Shimane University, Matsue, Shimane 690-8504, Japan*

<sup>6</sup>*Graduate School of Life Sciences, Tohoku University, Sendai, Miyagi 980-8578, Japan*

<sup>7</sup>*National Research Institute of Fisheries Science, Japan Fisheries Research and Education Agency,  
2-12-4 Fukuura, Kanazawa, Yokohama, Kanagawa 236-8648, Japan*

<sup>8</sup>*Laboratory of Animal Ecology, Department of Zoology, Graduate School of Science, Kyoto University,  
Kyoto 606-8502, Japan*

<sup>9</sup>*Field Science Center for Northern Biosphere, Hokkaido University, Hakodate, Hokkaido 040-0051, Japan*

<sup>10</sup>*Graduate School of Human Development and Environment, Kobe University, Kobe, Hyogo 657-8501, Japan*

\*fukaya.keiichi@nies.go.jp

\*\*michio.kondo.b8@tohoku.ac.jp

## 5 **Abstract**

6 Molecular analysis of DNA left in the environment, known as environmental DNA  
7 (eDNA), has proven to be a powerful and cost-effective approach to infer  
8 occurrence of species. Nonetheless, relating measurements of eDNA concentration  
9 to population abundance remains difficult because detailed knowledge on the  
10 processes that govern spatial and temporal distribution of eDNA should be  
11 integrated to reconstruct the underlying distribution and abundance of a target  
12 species. In this study, we propose a general framework of abundance estimation for  
13 aquatic systems on the basis of spatially replicated measurements of eDNA. The  
14 proposed method explicitly accounts for production, transport, and degradation of  
15 eDNA by utilizing numerical hydrodynamic models that can simulate the  
16 distribution of eDNA concentrations within an aquatic area. It turns out that,

17 under certain assumptions, population abundance can be estimated via a Bayesian  
18 inference of a generalized linear model. Application to a Japanese jack mackerel  
19 (*Trachurus japonicus*) population in Maizuru Bay revealed that the proposed  
20 method gives an estimate of population abundance comparable to that of a  
21 quantitative echo sounder method. Furthermore, the method successfully identified  
22 a source of exogenous input of eDNA (a fish market), which may render a  
23 quantitative application of eDNA difficult to interpret unless its effect is taken into  
24 account. These findings indicate the ability of eDNA to reliably reflect population  
25 abundance of aquatic macroorganisms; when the “ecology of eDNA” is adequately  
26 accounted for, population abundance can be quantified on the basis of  
27 measurements of eDNA concentration.

28 *Key words: Abundance estimation, Environmental DNA, Japanese jack mackerel*  
29 *(Trachurus japonicus), Quantitative echo sounder, Quantitative PCR, Tracer model*

## 30 Introduction

31 Knowledge of the distribution and abundance of species is crucial for ecology and related  
32 applied fields such as wildlife management and fisheries. In particular, quantitative  
33 assessments are often required to effectively monitor and manage ecosystems because trends in  
34 environmental stressors such as climate change, habitat modification, and pollution can result  
35 in shifts in the distribution and the level of population abundance of species. Nevertheless,  
36 quantification of natural population of species can be challenging, if not impossible, at least  
37 due to the extensive effort required for field survey and the low detection probability of species  
38 or individuals (Yoccoz et al. 2001).

39 The detection and quantification of environmental DNA (eDNA) is an emerging  
40 methodology for ecological studies and could enhance the ability of investigators to infer  
41 occurrence and abundance of species. This approach has been applied, especially but not  
42 exclusively, to aquatic species such as fish and amphibians and has been identified as a powerful  
43 and yet cost-effective tool for species detection (Bohmann et al. 2014, Rees et al. 2014,  
44 Thomsen and Willerslev 2015, Goldberg et al. 2016, Deiner et al. 2017, Hansen et al. 2018).

45 Challenges remain, however, in quantitative applications of eDNA. Since earlier studies  
46 revealed positive correlations between species abundance and eDNA concentration (Takahara  
47 et al. 2012, Thomsen et al. 2012, Goldberg et al. 2013, Pilliod et al. 2013, Eichmiller et al.  
48 2014), it has been expected that local population abundance may be inferred by measuring the  
49 concentration of eDNA at a given locality. Indeed, an analytical framework proposed for  
50 eDNA-based abundance estimation assumes a probability distribution that represents the  
51 quantitative relation between eDNA concentration and the underlying population size  
52 (Chambert et al. 2018). A recent empirical study showed that the abundance of anadromous  
53 fish in a river can be quantified based on frequent measurements of eDNA concentration, when  
54 streamflow is taken into consideration (Levi et al. 2019). Nonetheless, such a definite relation  
55 may not always be present, possibly depending on e.g., the shedding rate, transport, and  
56 exogenous input of eDNA (Pilliod et al. 2013, Eichmiller et al. 2014, Lacoursière-Roussel et al.  
57 2016, Yamamoto et al. 2016, Jo et al. 2017), especially in natural environments as indicated by

58 a meta-analysis (Yates et al. 2019).

59         The fundamental factors that underlie such context dependency are the “ecology of  
60 eDNA”: the distribution of eDNA in space and time stems from processes governing the origin,  
61 state, transport, and fate of eDNA particles (Barnes and Turner 2016). Thus, in applications  
62 of the eDNA methodology, detailed information about such processes may be critical. Without  
63 relevant knowledge of these processes, for example, the spatial and temporal scales of  
64 information provided by eDNA remain largely uncertain (Thomsen and Willerslev 2015,  
65 Goldberg et al. 2016, Hansen et al. 2018). Therefore, here, our purpose was to develop a  
66 general approach to eDNA-based abundance estimation that can fully account for the ecology  
67 of eDNA, i.e., the rate of production and degradation of eDNA as well as the transport of  
68 eDNA within a flow field in an aquatic area of interest (Figure 1). Although quantitative  
69 models of eDNA in which these processes are explicitly accounted for have been proposed for  
70 linear habitats such as rivers (Sansom and Sassoubre 2017, Carraro et al. 2018), no such model  
71 is currently available for general aquatic systems, including the marine environment.

72         In this study, we make use of a *tracer model*, namely, a numerical hydrodynamic model  
73 that can simulate the distribution of eDNA concentrations within an aquatic area (Shulman  
74 et al. 2003). Under certain assumptions, the behavior of the model can also be regarded  
75 mathematically as a linear function of an input vector representing the distribution of  
76 population abundance levels (densities) within the area. We show that the estimation of  
77 population abundance can then be achieved via a Bayesian inference of a generalized linear  
78 model (Figure 1). We applied this approach to a population of the Japanese jack mackerel  
79 (*Trachurus japonicus*, a commercially important fish species) in Maizuru Bay, Japan (Figure  
80 2). On the basis of the eDNA concentration measurements and a tracer model configured for  
81 Maizuru Bay, we obtained an estimate of fish population abundance in the bay. This estimate  
82 was then verified via a parallel estimate of abundance obtained by a quantitative echo sounder  
83 method. The results suggest that the proposed approach can reliably quantify fish population  
84 abundance in the bay.

## 85 **Materials and Methods**

### 86 **A general framework for abundance estimation**

#### 87 **The tracer model as a linear function**

88 Here, we define a *tracer model* as a numerical hydrodynamic model that simulates generation,  
89 transport, and decay of particles (i.e., eDNA) on the basis of a flow field determined by given  
90 physical conditions within an aquatic area of interest. In this study, we assume a tracer model  
91 for a three-dimensional discrete space in which the entire aquatic area of interest is discretized  
92 into grid cells of known volume. A tracer model can in principle simulate the ecology of eDNA  
93 and thus derives a spatial distribution of eDNA within the aquatic area, given that per capita  
94 and unit time shedding rates of eDNA, degradation rates of eDNA, and density (or  
95 equivalently, abundance) of organisms in each grid cell are specified, in addition to the flow  
96 field (Figure 1). The main idea that underlies the framework we propose is that we can regard  
97 a tracer model as a function that takes a vector of cell level density of organisms as an input  
98 and outputs eDNA concentration in each grid cell at a point in time; thus, the inference of  
99 abundance is an inverse problem: finding an input vector of a tracer model (i.e., density of  
100 organisms in each grid cell) that best explains measurements of eDNA concentration that are  
101 collected at a point in time and are replicated spatially within the aquatic area of interest.

102         Nevertheless, such a problem is difficult to solve under the general conditions where  
103 both the environment and abundance vary in a complex manner. We therefore make several  
104 key assumptions that simplify the problem (Figure 1). First, we assume that during two time  
105 points  $t$  and  $s$  ( $s < t$ ), key environmental variables for hydrodynamic processes are known from  
106 some observations and/or model prediction so that the flow field can be determined and  
107 plugged in to the tracer model. Here,  $t$  refers to the point in time at which eDNA  
108 concentration is observed at multiple locations within the aquatic area, and  $s$  denotes some  
109 point in time sufficiently far away from  $t$  such that eDNA concentration at  $t$  is virtually  
110 independent from that at  $s$ . Operationally,  $s$  and  $t$  define the time domain of the tracer model.  
111 Second, we assume that the rates of production and degradation of eDNA are known in each

112 grid cell during the period between  $s$  and  $t$ . They may either be regarded as constant across  
 113 space and time or assumed to vary depending on known environmental variables, such as water  
 114 temperature, salinity, and pH, so that the rates of generation and disappearance of eDNA can  
 115 be determined completely in the tracer model. In addition, we assume that these rates are  
 116 independent of the eDNA concentration, and thus both production and degradation of eDNA  
 117 are linear processes. Third, we suppose that in each grid cell, all eDNA particles arise  
 118 exclusively from individuals of the target species that are identical in their eDNA-shedding  
 119 rate. Finally, we assume that abundance is stationary in each grid cell throughout the period  
 120 between  $s$  and  $t$  (i.e., the demographic closure assumption; Williams et al. 2002).

121 Under these assumptions, a tracer model can be regarded as a linear function. We  
 122 denote density of organisms in cell  $i$  ( $i = 1, \dots, M$ ) by  $x_i$  and define  $\mathbf{x} = (x_1, x_2, \dots, x_M)$ . Let  
 123 us denote the water volume of each cell by  $\mathbf{v} = (v_1, v_2, \dots, v_M)$  so that abundance in cell  $i$  and  
 124 in the whole aquatic area is expressed as  $v_i x_i$  and  $\mathbf{v}^\top \mathbf{x}$ , respectively (here,  $\mathbf{a}^\top$  means the  
 125 transpose of vector  $\mathbf{a}$ ). The tracer model predicts eDNA concentration in each grid cell at time  
 126 point  $t$  that results from the generation, advection, diffusion, and degradation of eDNA  
 127 occurring between  $s$  and  $t$  within a given flow field, which we denote (without an explicit index  
 128 of  $t$ ) by  $\mathbf{c} = (c_1, c_2, \dots, c_M)$ . If  $a_{ij}$  is defined as the (per unit density) contribution of cell  $j$  to  
 129 eDNA concentration in cell  $i$  at time  $t$ , then eDNA concentration can be expressed as  
 130  $c_i = a_{i1}x_1 + a_{i2}x_2 + \dots + a_{iM}x_M$ . If we designate  $\mathbf{A} = (a_{ij})_{M \times M}$ , then this equation can be  
 131 written in a matrix form as  $\mathbf{c} = \mathbf{A}\mathbf{x}$ . Thus, although a tracer model indeed represents  
 132 temporal evolution of eDNA concentration within the period between  $s$  and  $t$  according to  
 133 some differential equations (presented below), its behavior can be described simply — under  
 134 the assumptions noted above — by matrix  $\mathbf{A}$ , which maps the vector of density  $\mathbf{x}$  onto the  
 135 vector of eDNA concentration  $\mathbf{c}$ . For  $i = 1, \dots, M$ , the  $i$ th column of  $\mathbf{A}$  can be obtained  
 136 numerically as a result of execution of the tracer model between time points  $s$  and  $t$  with a  
 137 vector of density in which cell  $i$  has a unit density and all other cells have null density.

138 **Fitting the tracer model to eDNA concentration data**

139 We assume that eDNA concentration was measured in  $N$  samples collected within the aquatic  
 140 area of interest at a point in time (or, in practice, within a sufficiently short period). Let us  
 141 denote the observed eDNA concentration in sample  $n$  by  $y_n$  ( $n = 1, \dots, N$ ) and express it with  
 142 vector  $\mathbf{y} = (y_1, \dots, y_N)$ . In the following text, we suppose that all eDNA measurements are  
 143 positive (i.e.,  $y_n > 0$ ). Note, however, that negative samples could also be included in the  
 144 analysis given that the detection process of eDNA is modeled jointly (Carraro et al. 2018). We  
 145 define  $i(n)$  as an index variable that means the index of the cell in which sample  $n$  was  
 146 obtained. If we let  $\mathbf{B} = (a_{i(n)j})_{N \times M}$ , the prediction of the tracer model for the data vector, as  
 147 a function of density vector  $\mathbf{x}$  is then expressed as  $\mathbf{B}\mathbf{x}$ .

148 Because the tracer model yields a linear predictor for  $\mathbf{y}$ , we can apply the (generalized)  
 149 linear modeling framework (McCullagh and Nelder 1989) to estimate density vector  $\mathbf{x}$ ; in  
 150 particular, we can regard  $\mathbf{B}$  and  $\mathbf{x}$  as a design matrix and a vector of coefficients of a linear  
 151 regression model, respectively (note that because  $\mathbf{x}$  represents density, the searches for  
 152 estimates should be within the space of parameters such that  $x_i \geq 0$  for all  $i$ ). Considering  
 153 that eDNA concentration data often represent a lognormal error structure (e.g., Takahara  
 154 et al. 2012, Thomsen et al. 2012, Eichmiller et al. 2014, Wilcox et al. 2016, Jo et al. 2017), we  
 155 can consider the following model:

$$\log \mathbf{y} \sim \mathcal{N}(\log \mathbf{B}\mathbf{x}, \sigma^2 \mathbf{I}_N), \quad (1)$$

156 where  $\mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$  is a multivariate normal distribution with mean vector  $\boldsymbol{\mu}$ , and covariance  
 157 matrix  $\boldsymbol{\Sigma}$ ;  $\sigma^2$  is a residual variance, and  $\mathbf{I}_m$  is a  $m \times m$  identity matrix. Note that this is a  
 158 generalized linear model with an exponential link function (McCullagh and Nelder 1989). The  
 159 maximum likelihood method for this model yields an estimate  $\hat{\mathbf{x}}$  that minimizes the residual  
 160 square error  $\|\log \mathbf{y} - \log \mathbf{B}\hat{\mathbf{x}}\|_2^2$ .

161 The standard maximum likelihood approach is, however, not applicable to this model  
 162 when  $M > N$  because the maximum likelihood estimate of  $\mathbf{x}$  is not uniquely identified in this  
 163 setting. This may be a typical situation at a reasonable level of spatial discretization for the

164 tracer model and sampling effort of eDNA. Additional assumption (or regularization) on the  
165 regression coefficients is necessary to make an inference based on such a singular model. We  
166 can apply a Bayesian approach in which a common probability distribution is specified on  $\boldsymbol{x}$  as  
167 a prior distribution. This approach effectively specifies  $\boldsymbol{x}$  as random effects, allowing to  
168 “borrow strength” to estimate each element of  $\boldsymbol{x}$  (Kéry and Schaub 2012). Alternatively, when  
169 some covariates, assumed to covary with density, are available for each cell, an additional  
170 model component for density can be introduced to effectively reduce the number of unknown  
171 parameters (Carraro et al. 2018). Specifically, density of the target species can be modeled, for  
172 example, as  $\log \boldsymbol{x} = \boldsymbol{Z}\boldsymbol{\beta}$ , where  $\boldsymbol{Z}$  is a matrix of covariates, and  $\boldsymbol{\beta}$  is a vector of coefficients  
173 (including an intercept). Note, however, that the addition of a nonlinear component for  
174 density takes the model beyond the standard generalized linear modeling framework.

## 175 **An application to a marine fish population**

### 176 **Measurement of jack mackerel eDNA in Maizuru Bay**

177 The study was conducted in Maizuru Bay (Kyoto prefecture, Japan; 35°29'N, 135°23'E) to  
178 estimate abundance of the jack mackerel (*T. japonicus*) via concentration of eDNA. The bay  
179 has a surface area of  $\sim 22.87$  km<sup>2</sup> with a maximum water depth of approximately 30 m, and  
180 connects with Wakasa Bay through a narrow bay mouth in its north (Figure 2).

181 According to long-term underwater visual surveys, the jack mackerel is numerically the  
182 most dominant fish species in shallow (< 10 m in depth) coastal waters in this area (Masuda  
183 2008); their body size ranges from 10 to 45 mm in standard length offshore and 40–120 mm  
184 standard length in the shallow rocky reef habitat (Masuda et al. 2008). The study was  
185 conducted during the peak season of jack mackerel recruitment from the offshore pelagic zone  
186 to a coastal shallow reef habitat, where the jack mackerel population in the bay is dominated  
187 by new recruits. In the following analysis, we therefore assumed that the population is  
188 represented by individuals of size  $\sim 3$  cm (body length) and  $\sim 1$  g (body weight; see Appendix  
189 S1, Supporting information).

190 We conducted the water sampling on 21 and 22 June 2016 from a research vessel at 100  
191 stations located approximately on  $\sim 400$  m grids in Maizuru Bay (Figure 2). At each sampling

192 station, we captured a 1-L sea water sample at three depths: the surface, middle, and bottom.  
193 The middle and bottom depths were defined as 5 m from the surface, which was just below the  
194 pycnocline, and 1 m above the sea floor, respectively. We filtered water samples on the same  
195 day of the field survey, which were then subjected to eDNA extraction and subsequent  
196 quantitative PCR (qPCR). qPCR was carried out in triplicate for each sample. Details of the  
197 measurement of eDNA concentration are fully described in Appendix S2, Supporting  
198 information.

### 199 **Development of the eDNA tracer model**

200 To obtain the flow field in Maizuru Bay, we configured the Princeton Ocean Model (POM)  
201 with a scaled vertical coordinate (i.e., the sigma coordinate system, in which the number of  
202 layers of the water column is the same for every grid irrespective of the sea depth; Mellor 2002)  
203 for the bay. The model represented Maizuru Bay by 20,484 grid cells. Specifically, the bay was  
204 discretized by 2,276 horizontal lattice grids at a resolution of 100 m, and the grids had nine  
205 non uniform vertical layers, with finer resolution near the surface; the boundary of each layer  
206 in the sigma coordinate was set as  $\sigma = 0.000, -0.041, -0.088, -0.150, -0.245, -0.374,$   
207  $-0.510, -0.646, -0.796,$  and  $-1.000$ . The configuration of the model was achieved by means  
208 of the bottom topography of the bay, data and model estimates of surface meteorological  
209 conditions, estimated river discharges, and the model results of Wakasa Bay as the open  
210 boundary conditions (Yoon and Kasai 2017); additional details are described in Appendix S3.  
211 The model simulated flow fields within the bay from 1 June 2016, under the initial conditions  
212 interpolated from the model results of Yoon and Kasai (2017), to the final day for the water  
213 sampling (i.e., 22 June 2016). The time steps of the simulation were set to 0.1 s for the  
214 external mode to update the surface elevation and vertically averaged velocities, whereas they  
215 were 3 s for the internal mode to update the horizontal velocities, potential temperature,  
216 salinity, and turbulence quantities (Mellor 2002).

217 The concentration of eDNA of jack mackerels was then simulated based on the flow  
218 fields produced by the POM. The evolution of eDNA concentration, denoted by  $c$ , is  
219 represented as

$$\frac{\partial c}{\partial t} + u\nabla(c) = \nabla^*(d\nabla(c)) - \lambda c + \beta x, \quad (2)$$

220 where  $u$  is a three-dimensional velocity vector,  $\nabla(c)$  is the gradient of  $c$ ,  $\nabla^*(\cdot)$  is the divergence  
 221 operator,  $d$  is a vector of diffusion coefficients,  $\lambda$  is a degradation rate of eDNA,  $\beta$  is a  
 222 per-capita shedding rate of jack mackerel DNA, and  $x$  is the density of jack mackerels in the  
 223 cell. The eDNA degradation rate was assumed to be constant and was adopted from an  
 224 estimate obtained in tank experiments where the same species-specific primer set was  
 225 employed ( $\lambda = 0.044 \text{ h}^{-1}$ ; Jo et al. 2017). The eDNA shedding rate of the jack mackerel was  
 226 assumed to be constant; it was derived mathematically and found to be  $\beta = 9.88 \times 10^4$  copies  
 227 per individual per hour, according to the results of tank experiments conducted by Maruyama  
 228 et al. (2014) and Jo et al. (2017). Details of this derivation are provided in Appendix S4,  
 229 Supporting information. The settling and resuspension of eDNA particles were ignored in Eq.  
 230 2 given that little is known about the rate of these processes.

231 For each of the 20,484 columns of the  $\mathbf{A}$  matrix, the tracer model was executed from 1  
 232 June 2016 to 22 June 2016 to generate the values of the column elements. The elements in  $\mathbf{A}$   
 233 were specified by the daily averages on 22 June and then used in the subsequent analyses.

### 234 **Estimation of jack mackerel abundance based on the eDNA tracer model**

235 We fitted the model with lognormal error distribution (Eq. 1) to the eDNA concentration data  
 236 collected in Maizuru Bay. During the model fitting, we omitted negative samples in which the  
 237 number of remaining observations was  $N = 729$ . For vector of density  $\mathbf{x}$ , we specified an  
 238 independent lognormal prior with unknown prior mean  $\mu$  and standard deviation  $\tau$ :

$$\log \mathbf{x} \sim \mathcal{N}(\log \mu \mathbf{1}_M, \tau^2 \mathbf{I}_M), \quad (3)$$

239 where  $\mathbf{1}_M$  represents a vector of all ones with length  $M$ . Because  $N$  was significantly smaller  
 240 than  $M$ , we were pessimistic about estimating the spatial variation in cell level density with  
 241 reasonable precision. Our main goal of the inference was therefore to quantify the bay-level  
 242 abundance  $\mathbf{v}^\top \mathbf{x}$  along with its uncertainty.

243 With uniform positive priors on  $\mu$ ,  $\tau$ , and  $\sigma$ , we fitted the model via a fully Bayesian  
244 approach. Posterior samples were obtained by the Markov chain Monte Carlo (MCMC)  
245 method implemented in Stan (version 2.18.1; Carpenter et al. 2017) in which three  
246 independent chains of 10,000 iterations were generated after 1,000 warm-up iterations. Each  
247 chain was thinned at intervals of 10 to save the posterior sample.

248 Convergence of the posterior was checked for each parameter with the  $\hat{R}$  statistic.  
249 Posterior convergence was achieved at a recommended degree ( $\hat{R} < 1.1$ ; Gelman et al. 2013) in  
250 almost all parameters except  $\log x$  in four cells. We decided, however, that the results are solid  
251 because the posterior of the bay-level abundance — the target of the inference — fully  
252 converged. The goodness-of-fit assessment of the model, measured by the  $\chi^2$ -discrepancy  
253 statistic (Conn et al. 2018), gave no clear indication of a lack of model fit (Bayesian  $p$ -value:  
254 0.404).

255 We note that the independence assumption of the fitted model (Eq. 1) ignores the  
256 correlation between triplicates within each water sample, resulting in a potential  
257 underestimation of the uncertainty in the estimates of jack mackerel abundance. Although  
258 such a within-sample correlation could be accommodated in the model by explicitly accounting  
259 for the covariance structure of data, we here adopt the independence assumption for the  
260 purpose of illustrating the proposed framework.

## 261 **Estimation of jack mackerel abundance from quantitative echo sounder data**

262 An independent estimate of jack mackerel abundance was obtained based on a calibrated  
263 quantitative echo sounder by a standard acoustic survey method (Simmonds and MacLennan  
264 2005). The acoustic survey was conducted during the survey cruise for the water sampling  
265 (described above). We used the KSE300 echo sounder (Sonic Co. Ltd., Tokyo, Japan) with  
266 two transducers (T-182, 120 kHz, and T-178, 38 kHz; beam type, split-beam; beam width,  
267 8.5°; pulse duration, 0.3 ms; ping rate, 0.2 s), which were mounted off the side of the research  
268 vessel at a depth of 1 m. The acoustic devices were operated during the entire survey cruise to  
269 record all acoustic reflections, except when the research vessel stopped at each sampling  
270 station where the recording was stopped to avoid reflection from the sampling gear and cables.

271 The research vessel ran at  $\sim 4$  knots, on average, between the sampling stations. The echo  
 272 intensity data were denoised and cleaned in Echoview ver. 9.0 (Echoview Software Pty. Ltd.,  
 273 Tasmania, Australia). We omitted signals between the sea bottom and 0.5 m above it to  
 274 exclude the acoustic reflection from the sea floor. Additionally, we eliminated signals from sea  
 275 nettles (*Chrysaora pacifica*) by filtering reflections of  $-75$  dB.

276 From the obtained acoustic data, the reflections of jack mackerel were extracted by the  
 277 volume back scattering strength difference ( $\Delta S_V$ ) method (Miyashita et al. 2004, Simmonds  
 278 and MacLennan 2005).  $\Delta S_V$  was defined as the difference in the volume backscattering  
 279 strength ( $S_V$ ) between the two frequencies as follows:

$$\Delta S_V = S_{V120 \text{ kHz}} - S_{V38 \text{ kHz}}. \quad (4)$$

280 According to field validation in Maizuru Bay combining acoustic surveys and visual  
 281 confirmation of jack mackerel schools by snorkelling, we assumed the range of  $\Delta S_V$  of jack  
 282 mackerel between  $-6.4$  and  $5.2$  dB. This criterion discriminates the jack mackerel from larval  
 283 Japanese anchovy (*Engraulis japonicus*), the subdominant species in the bay (Masuda 2008),  
 284 which reflects the high frequency echo strongly as compared to low frequency (Ito et al. 2011)  
 285 and was used to determine  $S_V$  of the jack mackerel in  $1 \text{ m}^3$  water cubes.  $S_V$  values were  
 286 extracted for every 10 m segment of the survey line for every 1 m of depth using Echoview ver.  
 287 9.0.

288 Density of jack mackerel in a  $1 \text{ m}^3$  water cube, denoted by  $D$ , was obtained as

$$D = \frac{10^{\frac{S_{V120 \text{ kHz}}}{10}}}{10^{\frac{TS}{10}}} \quad (5)$$

289 where  $TS$  is the target strength of an individual jack mackerel. By assuming that jack  
 290 mackerel population in the bay was dominated by individuals of the size 3 cm, we chose  
 291  $TS = -59.6$  dB (Nakamura et al. 2013, Yamamoto et al. 2016). The fish density for each 10 m  
 292 segment and 1 m of depth on the echo sounder track lines was then matched with the grid  
 293 specification of the tracer model.

294 To obtain an estimate (and its associated uncertainty) of the bay-level abundance of

295 jack mackerel that can be compared to that obtained with the eDNA-based approach, a linear  
296 mixed model was fitted to the fish density data via a fully Bayesian approach. Details of the  
297 abundance estimation for quantitative echo sounder data are described in detail in Appendix  
298 S5, Supporting information.

## 299 Results

300 The proposed method yielded an estimate of fish abundance that was more than two times  
301 higher than the quantitative echo sounder estimate; although the point estimate of the eDNA  
302 method was of the same order of magnitude as the quantitative echo sounder estimate, there  
303 was no overlap in the two 95% highest posterior density intervals (HPDIs) (Table 1). In the  
304 eDNA method, however, we could identify a coordinate of grids in which density of jack  
305 mackerels was estimated to be unrealistically high; fish abundance in the nine vertical cells in  
306 this location was estimated at as much as tens of millions of individuals (posterior median and  
307 95% HPDI:  $1.35 \times 10^7$  [0.00 to  $1.77 \times 10^7$ ] individuals; Figure 2b). It is located next to a  
308 wholesale fish market (Figure 2a), which has been suspected as a significant source of  
309 exogenous jack mackerel eDNA in Maizuru Bay (Yamamoto et al. 2016, Jo et al. 2017). We  
310 therefore regarded the extreme estimates in these cells as resulting from a massive eDNA input  
311 from the market and excluded them from the inference of the bay-level fish abundance. This  
312 correction for the eDNA method reduced the estimate of fish abundance in the bay. As a  
313 result, the abundance estimates of the two methods become more comparable; the estimate  
314 corrected for the eDNA method was 1.42 times higher than the estimate via the quantitative  
315 echo sounder method, with the two 95% HPDIs overlapping (Table 1).

316 The eDNA concentration spatial distribution predicted by the fitted model  
317 corresponded well to the observed values (posterior median and 95% HPDI of the correlation  
318 coefficient: 0.652 [0.638 to 0.664]; Figures 3 and 4). Nevertheless, there was a high level of  
319 uncertainty in the estimate of fish density in each grid cell (Figure 2b), as expected given the  
320 small number of samples relative to the number of grid cells. As a result, neither a discernible  
321 spatial pattern of fish density nor a clear correlation between the estimates of the two methods  
322 was evident at the cell scale (Figure 5 and Supplementary Table S1).

323 To examine the robustness of the inference, we conducted an additional analysis in  
324 which fish density was estimated in coarser resolutions while using the same tracer model.  
325 Specifically, we fitted three model variants wherein coarser grid blocks are defined by  
326 aggregating horizontally neighboring cells at intervals of 200, 300, or 400 m, respectively, for  
327 each of which fish density was estimated (Supplementary Figure S1). The three model variants  
328 yielded an estimate of the bay-level fish abundance that are close to the original estimate  
329 (Supplementary Table S1). Moreover, they indicated an extremely high fish density in the grid  
330 blocks that are next to the fish market (Supplementary Figure S1). The estimates of the  
331 bay-level fish abundance, corrected for the fish market, were also similar to the original  
332 estimate (Supplementary Table S1). A better correlation was observed in coarser grid blocks  
333 between fish density estimated with the eDNA method and that estimated with the  
334 quantitative echo sounder method (Supplementary Table S1).

## 335 Discussion

336 The eDNA methods are rapidly developing technologies that have a great potential to  
337 facilitate the understanding and management of aquatic species, although their quantitative  
338 applications are still the critical step. This study presents a novel approach to abundance  
339 estimation based on quantitative eDNA measurements into which a numerical tracer model is  
340 incorporated to explicitly account for the details of the ecology of eDNA (Figure 1). Briefly, it  
341 requires the following steps: (1) Develop a hydrodynamic model for an aquatic area of interest.  
342 (2) Collect spatially replicated samples at a point of time from the aquatic area to measure  
343 eDNA concentration. (3) Configure the tracer model for the field measurement of eDNA; this  
344 will require knowledge of the rate of eDNA shedding and degradation. Then, run the tracer  
345 model repeatedly to obtain a design matrix of a generalized linear model that relates the  
346 underlying density to observed eDNA concentration. (4) Fit the generalized linear model to  
347 eDNA concentration data statistically, to estimate density of organisms for each discretized  
348 grid cell. This approach may be flexibly applied to a wide array of aquatic systems in which  
349 hydrodynamics and rates of eDNA shedding and degradation are modeled, thereby broadening  
350 the scope of the general idea implemented recently in a one-dimensional lotic system with a

351 single eDNA source (Sansom and Sassoubre 2017, Levi et al. 2019) and in a river network  
352 system with multiple eDNA sources (Carraro et al. 2018).

353 The application of the proposed approach to the Japanese jack mackerel population in  
354 Maizuru Bay indicated that abundance of species can be reliably estimated by means of eDNA  
355 in a coastal ecosystem, where oceanographic processes drive transportation of eDNA  
356 (Andruszkiewicz et al. 2019). Furthermore, the results revealed that the method can  
357 distinguish major exogenous sources of eDNA, which have been recognized as a nuisance factor  
358 in eDNA applications especially for species subject to fishery (Yamamoto et al. 2016, Jo et al.  
359 2017). These results suggest that when the processes of eDNA shedding, transport, and  
360 degradation were properly accounted for, an absolute estimation of abundance of aquatic  
361 macroorganisms can be practically achieved based on quantitative measurement of eDNA.

362 The proposed framework, however, has several limitations in its current form. For  
363 example, it requires several key assumptions, such as the stationarity (i.e., demographic  
364 closure) of the population and homogeneity of individuals in terms of their rate of eDNA  
365 shedding (Figure 1). This implies that the inferences can be biased by fluctuations in the  
366 spatial distribution of abundance, as well as heterogeneity in the shedding rate of eDNA  
367 and/or other factors that deviate from the modeling assumptions, if such factors are present.  
368 In addition, the number of eDNA samples may typically be smaller than the number of grid  
369 cells in the tracer model, thus requiring additional models describing among-cell variation in  
370 population density to make statistical inference (see *Materials and Methods*). Although our  
371 results indicated that the method can be applied even with these limitations, further  
372 methodological development would be warranted.

373 Ambiguity in the modeled processes could add further bias and uncertainty in the  
374 inferences based on a tracer model. The tracer model depends on the specified values for the  
375 rates of eDNA shedding and degradation, which have been quantified experimentally (e.g.,  
376 Maruyama et al. 2014, Sassoubre et al. 2016, Jo et al. 2017, Nukazawa et al. 2018, Jo et al.  
377 2019); yet our knowledge is still limited to predict them accurately, and even less is known  
378 about the difference between these rates in field and laboratory environments. Despite being  
379 ignored in our application, gravitational settling (and possibly, resuspension) of eDNA

380 particles may even have a significant effect on the spread of eDNA in a coastal ecosystem  
381 (Andruszkiewicz et al. 2019). However, little is known about the rates of these processes.  
382 Because the research on aquatic eDNA of macroorganisms is still in its infancy since its  
383 discovery (Ficetola et al. 2008), more work is needed to elucidate the processes that determine  
384 a distribution of eDNA in the field; a better understanding of the ecology of eDNA will  
385 improve the accuracy of quantitative eDNA approaches.

386 In our application, the local variation in fish density was not estimated reasonably; this  
387 is probably because the number of grid cells was too large relative to the number of eDNA  
388 samples. Given the logistical constraints in collecting eDNA samples, this may occur  
389 frequently in practical applications. A solution for better inference of local fish density may be  
390 to aggregate neighboring grid cells to yield coarser spatial units on which specific density is  
391 estimated. This approach may not only reduce the number of unknown quantities in the  
392 model, but it also may increase the likelihood that the assumption of population closure is  
393 met. In fact, we observed in our additional analysis an improved consistency in the estimated  
394 fish density obtained based on eDNA and the acoustic survey (Supplementary Table S1).  
395 Although it is computationally more challenging, specifying a prior distribution that explicitly  
396 accounts for spatial autocorrelation in fish density could be useful for obtaining smoothed  
397 estimates. When some relevant covariates are available for each spatial unit, spatial variation  
398 in density may be inferred more explicitly through an additional model component for local  
399 density (see *Materials and Methods*). As a possible alternative approach, eDNA measurements  
400 could be combined with classical protocols for abundance estimation to improve the inference  
401 on spatial variation in density (Chambert et al. 2018). However, it will require a further  
402 generalization of the model to formally accommodate different types of observations.

403 It has been argued that in an application of the eDNA method, careful consideration of  
404 details of the ecology of eDNA is critical (Bohmann et al. 2014, Rees et al. 2014, Thomsen and  
405 Willerslev 2015, Barnes and Turner 2016, Goldberg et al. 2016, Deiner et al. 2017, Hansen  
406 et al. 2018). We implemented this idea in a quantitative eDNA method, leading to integration  
407 of eDNA concentration measurements and hydrodynamic modeling for abundance estimation.  
408 The relatively less explored field of quantitative eDNA applications lies in the multispecies

409 context, which involves eDNA metabarcoding rather than the targeted quantitative PCR  
410 (qPCR) method (Deiner et al. 2017). The proposed approach would be applicable to the  
411 emerging quantitative metabarcoding technique (e.g., Ushio et al. 2018) in the same way, which  
412 may enable researchers to analyze many aquatic species at one time. Exploring between-species  
413 differences in the rate of eDNA shedding and degradation may therefore be worthwhile. In  
414 addition to remarkable efficiency in species detection, we expect that eDNA methodologies can  
415 enhance the ability of investigators to gain quantitative insights into aquatic ecosystems.

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557 198:225–235.

## 558 **Data accessibility**

559 The datasets and R/Stan scripts to generate the results are archived in Dryad  
560 (<https://doi.org/10.5061/dryad.f4qrfj6t7>).

## 561 **Authors' contributions**

562 M.K., R.M., A.K., K. Miyashita, and T.M. conceived and designed the eDNA survey. H.M.  
563 and S. Yamamoto conducted the molecular experiments. K. Minami and K. Miyashita  
564 analyzed the echo sounder data. S. Yoon and A.K. developed the tracer model. K.F. and Y.O.  
565 designed the methodology and conducted data analyses. K.F., H.M., S. Yoon, K. Minami, and  
566 A.K. led the writing of the manuscript. All the co-authors discussed the results and  
567 contributed critically to the manuscript.

Method	Abundance estimates	95% Bayesian credible interval
eDNA tracer model	$3.31 \times 10^7$	$(2.32 \times 10^7, 6.32 \times 10^7)$
(fish market cells omitted)	$2.23 \times 10^7$	$(0.77 \times 10^7, 5.29 \times 10^7)$
Quantitative echo sounder	$1.57 \times 10^7$	$(1.51 \times 10^7, 1.64 \times 10^7)$

Table 1. Estimates of Japanese jack mackerel abundance in Maizuru Bay. The second row of the eDNA method gives the abundance estimate that excluded the nine vertical cells next to the wholesale fish market (indicated in Figure 2a), which were identified as extraordinary eDNA sources. The point abundance estimates and credible intervals are presented as posterior medians and highest posterior density intervals, respectively. In both estimation methods, estimates are obtained under the assumption that the size of jack mackerel individuals was 3 cm in body length and 1 g in body weight (see Materials and Methods).

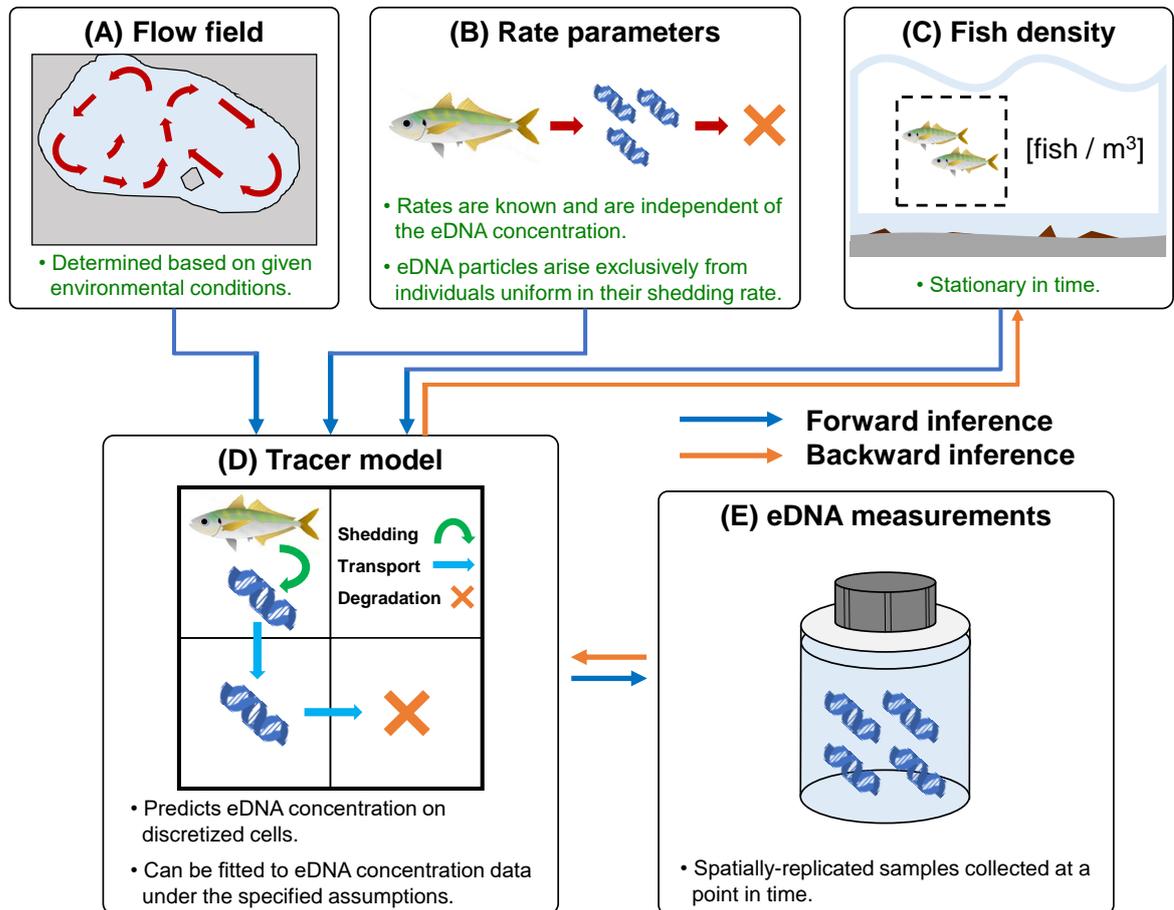


Fig. 1. Conceptual representation of the modeling framework. A tracer model (D) predicts the spatial distribution of eDNA concentration (E) within an aquatic area of interest under the specified flow field (A), rates of eDNA shedding and degradation (B), and spatial distribution of fish density (C). This is a forward inference of the model (blue arrows) represented by the governing equation (Eq. 2). Population density can be estimated by fitting the tracer model statistically to eDNA concentration measurements collected at a point of time within the modeled aquatic domain. This is a backward inference of the model (orange arrows) that can be achieved under the specified flow field and rate parameters in addition to some key assumptions described by green letters.

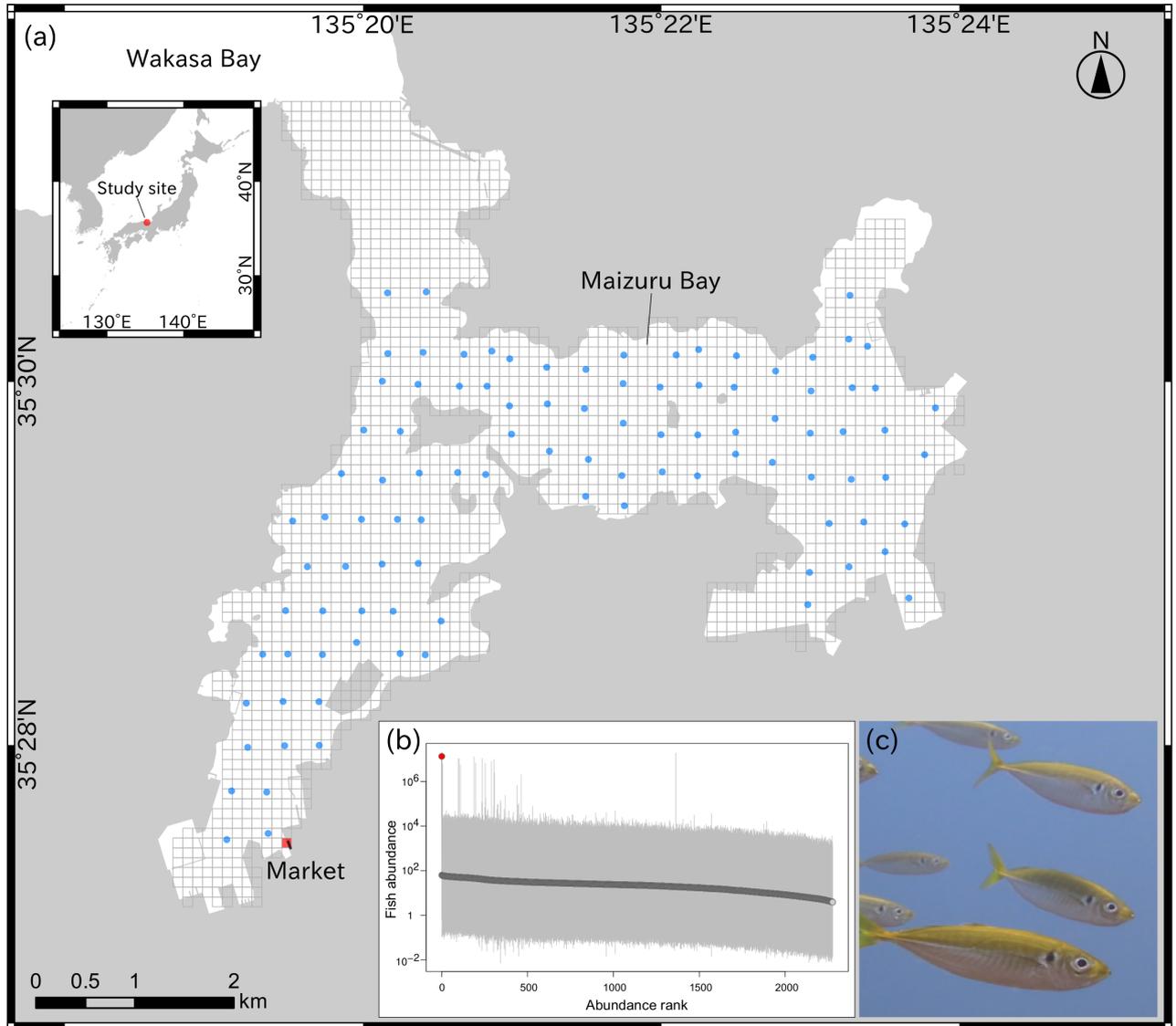


Fig. 2. Maizuru bay, the study site. (a) The 2,276 horizontal lattice grids for the eDNA tracer model (grey boxes) and the 100 water-sampling stations (blue circles). The grid in which estimates of jack mackerel density were extremely high is highlighted in red. The building of the fish market, overlapping with the red lattice grid, is depicted by a filled black box. (b) Fish abundance estimates (circles: posterior medians; bars: 95% highest posterior density intervals) in the 2,276 horizontal lattice grids. Abundance estimates in nine vertical cells were pooled for each grid. The lattice grid next to the market is highlighted in red. (c) The Japanese jack mackerel (*T. japonicus*) in Maizuru bay (photo credit: R. Masuda).

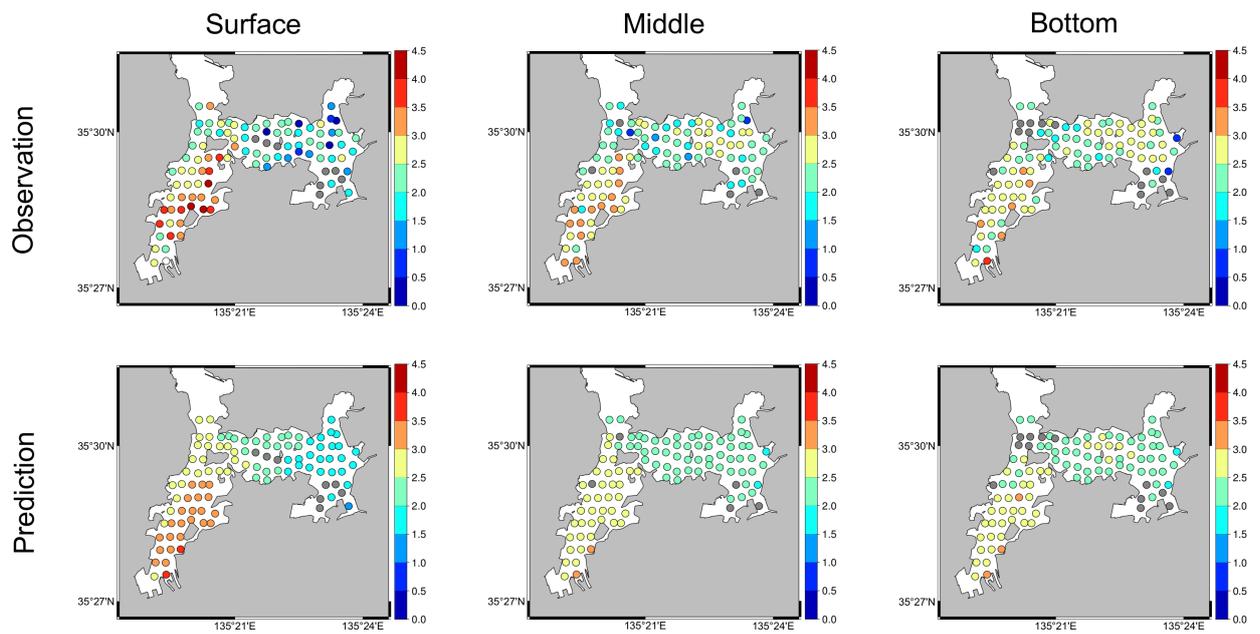


Fig. 3. Observed (upper panels) and predicted (lower panels) spatial distribution of eDNA concentration in 100 sampling locations. Left, center, and right panels show eDNA concentration at the surface, middle, and bottom layer, respectively. The color of each point represents the logarithm of eDNA concentration (copies/L) to base 10. The average concentration of positive samples was used for observed values. Posterior medians were used for predicted values. For visualization purposes, data collected from the surface layer of a station next to a wholesale fish market were omitted. Gray points indicate stations with only negative samples.

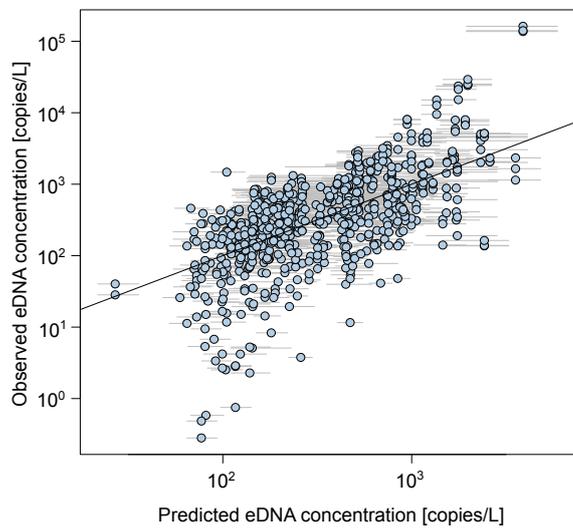


Fig. 4. Posterior predicted value and observed value of eDNA concentration in all samples. For predicted values, the posterior medians and 95% highest posterior density intervals are represented by circles and horizontal bars, respectively. The crossed line is the identity line.

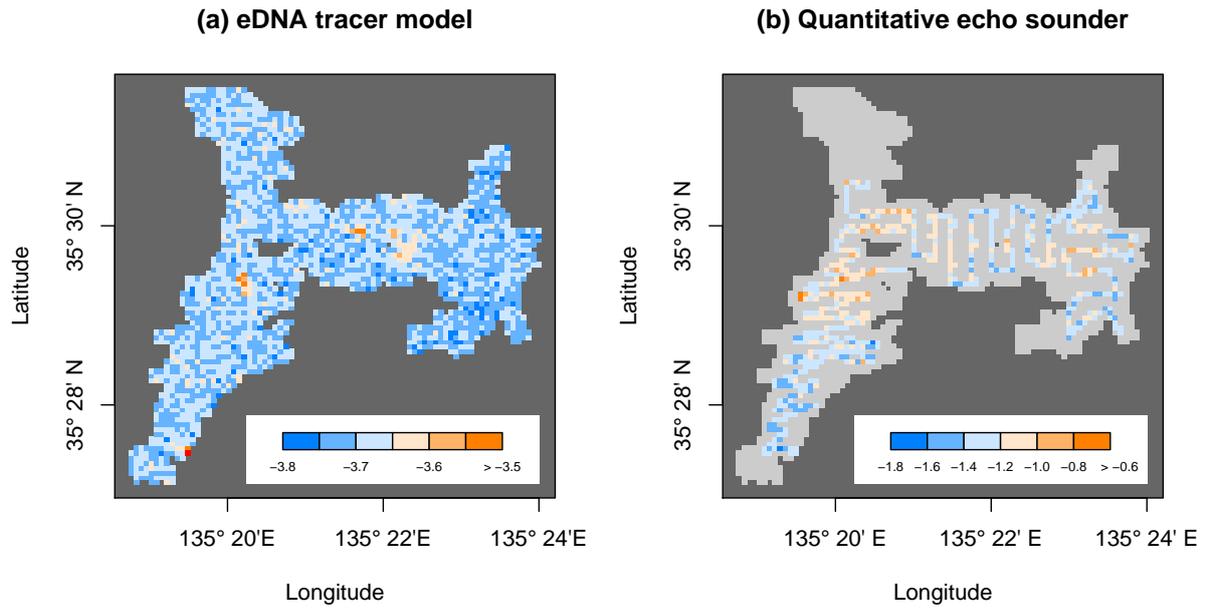


Fig. 5. Spatial distribution of density of Japanese jack mackerel estimated using (a) the proposed method and (b) the quantitative echo sounder method. Each panel shows the estimated density (posterior median) in the horizontal lattice grids, in which the colors represent the logarithm of fish density (individuals per  $1 \text{ m}^3$ ) to base 10. Note the difference in the color scales. The uppermost color categories include a small number of outliers. In panel (a), the grid cell next to the fish market with an extremely high estimated density is highlighted in red. In panel (b), the horizontal lattice grids without quantitative echo sounder data are shown in gray.